

Probing the high momentum component of the deuteron at high Q^2

W.U. Boeglin,¹ L. Coman,¹ P. Ambrozewicz,¹ K. Aniol,² J. Arrington,³ G. Batigne,⁴ P. Bosted,⁵
 A. Camsonne,⁵ G. Chang,⁶ J.P. Chen,⁵ S. Choi,⁷ A. Deur,⁵ M. Epstein,² J.M. Finn,^{8,*} S. Frullani,⁹
 C. Furget,⁴ F. Garibaldi,⁹ O. Gayou,^{10,5} R. Gilman,^{10,5} O. Hansen,⁵ D. Hayes,¹¹ D.W. Higinbotham,⁵
 W. Hinton,¹¹ C. Hyde,¹¹ H. Ibrahim,^{12,11} C.W. de Jager,⁵ X. Jiang,¹⁰ M. K. Jones,⁵ L.J. Kaufman,^{13,†}
 A. Klein,¹⁴ S. Kox,⁴ L. Kramer,¹ G. Kumbartzki,¹⁰ J.M. Laget,⁵ J. LeRose,⁵ R. Lindgren,¹⁵
 D.J. Margaziotis,² P. Markowitz,¹ K. McCormick,¹⁶ Z. Meziani,⁷ R. Michaels,⁵ B. Milbrath,⁵
 J. Mitchell,^{5,‡} P. Monaghan,¹⁷ M. Moteabbed,¹ P. Moussiegt,⁴ R. Nasseripour,¹ K. Paschke,¹⁵
 C. Perdrisat,⁸ E. Piasetzky,¹⁸ V. Punjabi,¹⁹ I.A. Qattan,^{20,3} G. Quémener,⁴ R.D. Ransome,¹⁰ B. Raue,¹
 J.S. Réal,⁴ J. Reinhold,¹ B. Reitz,⁵ R. Roché,²¹ M. Roedelbronn,²² A. Saha,^{5,*} K. Slifer,²³ P. Solvignon,³
 V. Sulkosky,^{5,§} P.E. Ulmer,^{11,‡} E. Voutier,⁴ L.B. Weinstein,¹¹ B. Wojtsekhowski,⁵ and M. Zeier¹⁵

(For the Hall A Collaboration)

¹Florida International University, University Park, Florida 33199

²California State University, Los Angeles, Los Angeles, California 90032

³Argonne National Laboratory, Argonne, Illinois 60439

⁴LPSC, Université Joseph Fourier, CNRS/IN2P3, INPG, Grenoble, France

⁵Thomas Jefferson National Accelerator Facility, Newport News, Virginia 23606

⁶University of Maryland, College Park, Maryland 20742

⁷Temple University, Philadelphia, Pennsylvania 19122

⁸College of William and Mary, Williamsburg, Virginia 23187

⁹INFN, Sezione Sanita and Istituto Superiore di Sanita, Laboratorio di Fisica, I-00161 Rome, Italy

¹⁰Rutgers, The State University of New Jersey, Piscataway, New Jersey 08854

¹¹Old Dominion University, Norfolk, Virginia 23529

¹²Physics Department, Faculty of Science, Cairo University, Giza 12613, Egypt.

¹³University of Massachusetts Amherst, Amherst, Massachusetts 01003

¹⁴Los Alamos National Laboratory, Los Alamos, New Mexico 87545

¹⁵University of Virginia, Charlottesville, Virginia 22901

¹⁶Kent State University, Kent, Ohio 44242

¹⁷Hampton University, Hampton, Virginia 23668

¹⁸University of Tel Aviv, Tel Aviv, Israel

¹⁹Norfolk State University, Norfolk, Virginia 23504

²⁰Northwestern University, Evanston, Illinois 60208

²¹Ohio University, Athens, Ohio 45701

²²University of Illinois, Urbana Champaign, Illinois 61820

²³The University of New Hampshire, Durham, New Hampshire 03824

(Dated: January 26, 2013)

The $^2H(e,e'p)n$ cross section at a momentum transfer of 3.5 (GeV/c)^2 was measured over a kinematical range that made it possible to study this reaction for a set of fixed missing momenta as a function of the neutron recoil angle θ_{nq} and to extract missing momentum distributions for fixed values of θ_{nq} up to 0.55 GeV/c . In the region of $35^\circ \leq \theta_{nq} \leq 45^\circ$ recent calculations, which predict that final state interactions are small, agree reasonably well with the experimental data. Therefore these experimental reduced cross sections provide direct access to the high momentum component of the deuteron momentum distribution in exclusive deuteron electro-disintegration.

PACS numbers: 25.30.Fj, 25.10+v, 25.60.Gc

The understanding of the short-range structure of the deuteron is of fundamental importance for the advancement of our understanding of nuclear matter at small

distances. To probe the short-range properties of the deuteron, one has to investigate configurations where the two nucleons come very close together and are strongly overlapping. The basic problem is to what extent these configurations can be described simply in terms of two nucleons with high initial relative momenta. The ultimate quantity to be investigated in this case is the high momentum component of the deuteron wave function. Traditionally three classes of reactions are used to study the high momentum part of the deuteron wave function: elastic scattering, inclusive and exclusive electro-

*deceased

†present address: Indiana University, Bloomington, Indiana 47405

‡present address: Renaissance Technologies LLC, East Setauket, New York 11733

§present address: Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

disintegration reactions.

Elastic electron-deuteron scattering probes the integrated characteristics of the wave function via the deuteron form-factors. At large 4-momentum transfer, $-Q^2$, the scattering becomes sensitive to the high momentum component of the deuteron wave function. The analysis of experimental data [1] showed that, at presently available energies, it is practically impossible to discriminate between different theoretical approaches [2, 3] used to calculate the deuteron elastic form-factor $A(Q^2)$. One needs additional constraints on the deuteron wave function at short distances.

Inclusive, quasi-elastic (e, e') reactions provide another way of probing high momentum components of the deuteron especially at high Q^2 and in the $x_B \geq 1$ region [4–7] where $x_B = Q^2/2M\nu$ (M is the nucleon mass and ν is the energy of the virtual photon) is the Bjorken scaling variable. In this regime the cross section depends on an integral of the deuteron momentum distribution with the longitudinal nucleon momentum component (with respect to the virtual photon momentum \vec{q}) as the lower limit. However, the difficulties of ensuring small contributions from inelastic processes (growing with Q^2) and final state interactions (FSI) at large x_B (see e.g. [8, 9]), reduce the sensitivity to the deuteron wave function at short inter-nucleon distances, although the high-momentum component is certainly important in this kinematics.

The most direct way of studying high nucleon momenta is to investigate the quasi-elastic (QE) electrodisintegration of the deuteron via the $^2H(e, e'p)n$ reaction at high missing momenta (the momentum of the recoiling neutron) $\vec{p}_m = \vec{q} - \vec{p}_f$, where \vec{p}_f is the momentum of the outgoing, observed proton. Within the Plane Wave Impulse Approximation (PWIA) $-\vec{p}_m$ corresponds to the initial momentum of the target nucleon before the interaction. Thus the strategy in these studies is to probe the cross section at p_m values as large as possible. However, depending on the selected kinematics, these studies can be overwhelmed by final state interactions (FSI) where the outgoing proton interacts with the recoiling neutron, or by processes where the virtual photon couples to the exchanged meson (MEC) or where the nucleon is excited to an intermediate Δ state (IC). The dominance of FSI, MEC and IC has seriously affected previous experiments at $Q^2 < 1$ (GeV/c)² [10–14] leading to the overall conclusion that these experiments do not provide good constraints on the high momentum components of the deuteron wave function.

The condition $Q^2 \geq 1$ (GeV/c)² is necessary in order to enhance contributions of reaction mechanisms which probe the short-range structure of the deuteron and to suppress competing long range processes for the following reasons: (i) the MEC contribution should be suppressed by an additional factor of $(1 + Q^2/\Lambda)^{-4}$ with $\Lambda = 0.8 - 1$ (GeV/c)² as compared to the QE contribution [15, 16]; (ii) the large Q^2 limit should allow one to probe the wave function in the $x > 1$ region which

is far from the inelastic threshold, thereby suppressing IC contributions; (iii) final state interactions of the outgoing nucleon should follow the eikonal dynamics with a strong angular anisotropy dominating mainly in transverse directions. This situation generated a multitude of theoretical studies of the $^2H(e, e'p)n$ reaction in the high Q^2 regime [15, 17–27]. The PWIA results of calculations described in ref. [15, 19, 22, 25, 27] differ at larger p_m due to differences in the wave functions and in details of the off-shell electron nucleon interaction used, but all predict small FSI contributions (10 - 20%) for $35^\circ \leq \theta_{nq} \leq 45^\circ$.

We report new $^2H(e, e'p)n$ cross sections measured at high momentum transfer for well defined kinematic settings. The wide range in missing momenta and neutron recoil angles allows one for the first time to access the high momentum components of the deuteron momentum distribution and probe the validity of current models of the reaction dynamics. The kinematic region covered overlaps with a recent $^2H(e, e'p)n$ experiment performed using CLAS at Jefferson Lab [28] which concluded that FSI and IC are dominating the momentum distribution except for $p_m < 0.1$ GeV/c or $\theta_{nq} > 110^\circ$. However, to obtain reasonable statistical precision, the data were integrated over the full θ_{nq} range for the momentum distributions and over a large p_m -range for the angular distributions in contrast to the data presented below.

At a fixed $Q^2 = 3.5$ (GeV/c)², the $^2H(e, e'p)n$ cross section was measured for specific missing momenta $p_m = 0.1, 0.2, 0.4, 0.5$ GeV/c, while the angle θ_{nq} of the recoiling neutron with respect to \vec{q} , was varied. θ_{nq} is also referred to hereafter as the recoil angle. For $p_m = 0.4, 0.5$ GeV/c, the largest recoil angles accessible were limited by the maximum momentum that the proton spectrometer was able to detect (3.1 GeV/c). Keeping p_m and Q^2 constant, required the energy transfer, the electron scattering angle, the proton final momentum and the proton direction to be adjusted accordingly for each value of θ_{nq} . As the energy transfer and recoil angle changed, x_B changed as well between 0.78 and 1.52, large x_B values corresponding to small recoil angles.

The experiment was carried out using the two high-resolution spectrometers in Hall A at Jefferson Lab at an electron beam momentum of 5.008 GeV/c. The left arm detected the electrons and the right arm the ejected protons. The deuterium target consisted of a 15 cm long cylinder filled with liquid deuterium and was part of the Hall A cryogenic target system [29]. An identical target cell filled with liquid hydrogen was used for calibration and to determine the coincidence efficiency. The electron beam was rastered over an area of 2×2 mm² and the liquids were continuously circulated in order to minimize density variations due to boiling. We found a typical reduction of the effective deuteron target thickness due to boiling by a factor of 0.94 ± 0.02 for an average current of 100 μ A. The cross sections were corrected for detector inefficiencies on a run-by-run basis and for an overall coincidence efficiency, determined from the measured $^1H(e, e')$ elastic cross section which was found to

be 96.4 ± 2 percent of the published value from the fit of Table I in ref. [30]. The systematic error due to uncertainties in the measured kinematic variables were calculated for each data bin and added quadratically to the statistical error. An overall error of 4.5 % was added to take into account errors in beam energy, beam charge measurements, detector efficiencies, target thickness and target boiling corrections.

The spectrometer detection systems in the two arms were very similar: vertical drift chambers (VDC) were used for tracking and two scintillation counter planes (S1/S2) following the VDCs provided timing and trigger signals. In addition, the electron arm was equipped with a gas Čerenkov detector for electron/ π^- discrimination. We found that the gas Čerenkov detector was sufficient for the π^- rejection in this experiment. At this large momentum transfer and at the large x_B kinematics the π^- background was not a concern. A detailed description of the spectrometer systems and the target system can be found in reference [29]. The momentum acceptance used for both spectrometers was set by software to $\delta = \Delta p/p_0 = \pm 4$ %, where p_0 is the central momentum of the spectrometer.

The solid angle of each spectrometer was defined by software cuts at the entrance of the first quadrupole magnet. In addition a second, global cut on the multi-dimensional acceptance of each spectrometer was applied by means of R-functions [31]. The phase space acceptance was calculated using the Hall A Monte-Carlo code MCEEP [32]. The extracted cross sections were radiatively corrected using the Monte-Carlo code SIMC [33, 34] where the yield was estimated with a theoretical calculation by J.M. Laget [25] that included final state interactions and reproduced the experimental yield quite well.

Several spectrometer settings contributed to a full angular distribution and the condition of constant Q^2 and constant p_m was maintained for the central setting only. Within the phase space acceptance defined by the two spectrometers the kinematic variables varied slightly around their central values as a function of the angle θ_{nq} . This led to variations of the experimental cross section as a function of θ_{nq} that were independent of reaction mechanism effects. In order to reduce these variations the experimental cross section was divided by the PWIA cross section $\sigma_{PWIA} = n_P(p_m)k\sigma_{cc1}$ where k is a kinematic factor, $n_P(p_m)$ refers to the Paris momentum distribution and σ_{cc1} is the de Forest CC1 off-shell cross section [35] calculated using the form factor parameterization from Table I of ref. [30]. Theoretical cross sections were calculated using the averaged kinematics determined for each bin in θ_{nq} , included bin center corrections and were divided by the same PWIA cross section as the experimental ones. The resulting ratios $R(\theta_{nq}) = \sigma_{exp}/\sigma_{pwia}$ were then averaged for overlapping θ_{nq} bins and the resulting angular distributions are shown in Fig. 1.

The angular distribution shown in Fig. 1a for missing momentum $p_m = 0.2 \pm 0.02$ GeV/c shows a clear reduc-

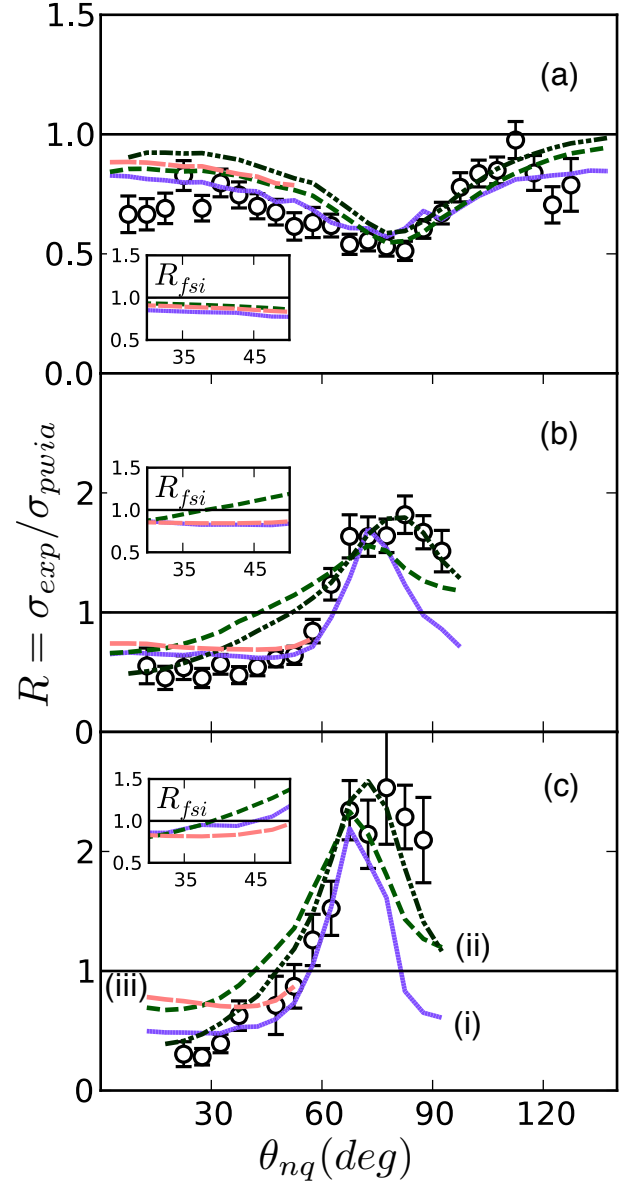


FIG. 1: (Color online) The ratio $R(\theta_{nq}) = \sigma_{exp}/\sigma_{pwia}$. (a) $p_m = 0.2$ GeV/c, (b) $p_m = 0.4$ GeV/c and (c) $p_m = 0.5$ GeV/c. Solid (purple) lines (i) MS [15, 19, 27] using the CD-Bonn potential, short dashed (green) lines (ii) JML [25], dashed-double-dot lines JML with MEC and IC and long-dashed (orange) lines (iii) JVO [22]. Insets: $R_{fsi} = \sigma_{fsi}/\sigma_{pwia}^{th}$ for $35^\circ \leq \theta_{nq} \leq 45^\circ$.

tion of R for θ_{nq} around 75° ($x_B \sim 1$). For missing momentum $p_m = 0.4 \pm 0.02$ GeV/c (Fig. 1b) and $p_m = 0.5 \pm 0.02$ GeV/c (Fig. 1c), R shows a peak at around 75° with a maximal value of ~ 1.6 and ~ 2.5 , respectively. The dependence of R on θ_{nq} reflects the angular dependence of final state interactions at high Q^2 . At high energies, FSI are described in the eikonal regime where the fast proton rescatters off the spectator neutron which in turn recoils almost perpendicularly to \vec{q} .

This measurement confirms the strong angular varia-

tion of the ${}^2H(e, e'p)n$ cross section as a function of θ_{nq} observed in the CLAS experiment [28] for missing momenta $0.4 \leq p_m \leq 0.6$ GeV/c. It is the basic feature under consideration in the study of the color transparency phenomenon in few-body systems [36].

Three different theoretical calculations were obtained: (1) a calculation by M. Sargsian [15, 19, 27], referred to as MS below, using the CD-Bonn or the Paris potentials, (2) cross sections from J-M. Laget's model [25], referred to as JML, using the Paris potential and (3) results from the model of Jeschonnek and Van Orden [22] which will be labelled JVO below. The relativistically covariant calculation of JVO is currently limited to small recoil angles.

The model predictions of $R = \sigma_{calc}/\sigma_{pwia}$ are compared to experimental data in Fig. 1. For small missing momenta ($p_m < 0.2$ GeV/c) and $\theta_{nq} < 30^\circ$ all calculations agree with each other within 20%. For larger angles and especially larger missing momenta, deviations between the experiment and the calculations and between the different calculations themselves are considerably larger. For $p_m = 0.4$ and 0.5 GeV/c MS correctly describes the rise of R with θ_{nq} , but predicts a faster fall-off after the maximum than is observed. JML predicts a considerably wider re-scattering peak. Including MEC and Δ excitation improves the agreement considerably at $p_m = 0.4, 0.5$ GeV/c (Fig. 1c) but worsens the agreement for $p_m = 0.2$ GeV/c (Fig. 1a). The value of the maximum agrees with experiment for both calculations. For $p_m = 0.4, 0.5$ GeV/c and $\theta_{nq} < 50^\circ$ MS and JVO describe the data considerably better than JML excluding MEC and Δ contributions. The ratio $R_{fsi} = \sigma_{fsi}/\sigma_{pwia}^{th}$, where σ_{fsi} is a calculated cross section including FSI and σ_{pwia}^{th} is the corresponding PWIA cross section, demonstrates that all calculations show relatively small contributions of FSI for $35^\circ < \theta_{nq} < 45^\circ$ (insets in Fig. 1). For $0.2 \leq p_m \leq 0.5$ GeV/c on average MS predicts between -18% and -5% FSI, JM between -9% and +5% and JVO between -12% and -16% FSI. This indicates a kinematic region where the cross section is dominated by PWIA and should therefore reflect directly the deuteron momentum distribution.

We extracted the ${}^2H(e, e'p)n$ cross section for three sets of fixed angles θ_{nq} with a bin width of $\pm 5^\circ$. For each of these three recoil angles, we determined the cross section as a function of missing momentum and calculated the reduced cross section $\sigma_{red} = \sigma_{exp}/(k\sigma_{cc1})$ using the same form factor as previously (Table I in ref. [30]). We included all spectrometer settings that contributed to the same (p_m, θ_{nq}) bin and determined the averaged, reduced cross section as well as the averaged kinematics. The theoretical cross sections have been treated the same way as the experimental ones. The resulting experimental momentum distributions are shown in Fig. 2.

The results for $\theta_{nq} = 75^\circ$ (Fig. 2c) show a typical behavior of reduced ${}^2H(e, e'p)n$ deuteron cross sections as a function of missing momentum, namely a 'flattening' of the cross section around $p_m > 0.3$ GeV/c. This flattening has been observed in most previous measurements

of the ${}^2H(e, e'p)n$ cross section at lower Q^2 which have been taken either at [13] $x_B \sim 1$, where FSI dominates or at values $x_B < 1$, where MEC and IC dominated [11]. From the measured angular distributions reported here and previously [28], we found that at this angle FSI contributions to the reaction are maximal.

The experimental reduced cross sections are compared to a calculation by M. Sargsian with wave functions from the CD-Bonn (i) and the Paris (ii) potentials. The PWIA results are shown as solid curves and the ones including FSI as dashed (CD-Bonn) and short dashed (Paris) lines. Both calculations at $\theta_{nq} = 75^\circ$ including FSI agree quite well with the measurement. The PWIA calculations cannot reproduce the data for $p_m > 0.1$ GeV/c and for $p_m > 0.45$ GeV/c the two calculations increasingly deviate from each other.

In contrast to $\theta_{nq} = 75^\circ$, the reduced cross sections $\theta_{nq} = 35^\circ$ and $\theta_{nq} = 45^\circ$, display a qualitatively different behavior as a function of p_m . The fall off is considerably steeper for $p_m > 0.3$ GeV/c and follows closely the general shape of the deuteron wave function in momentum space. At small θ_{nq} the calculated cross sections with FSI differ much less from the PWIA results and are sensitive to the type of NN potential used for $p_m > 0.45$ GeV/c.

We measured ${}^2H(e, e'p)n$ cross sections at a momentum transfer of 3.5 (GeV/c) 2 over a kinematical range that allowed us to study this reaction for a set of fixed missing momenta as a function of the neutron recoil angle θ_{nq} . We experimentally confirmed the validity of the generalized eikonal approximation which predicted a strong angular dependence of FSI contributions and kinematic regions where FSI contributions are small.

The small kinematic bin size made it possible for the first time to determine missing momentum distributions for several, fixed values of the neutron recoil angle, θ_{nq} and to observe a qualitative change in their shape. With decreasing θ_{nq} the momentum distributions change from the typical form found in previous experiments to a shape that follows more closely the trend of the deuteron wave function in momentum space. This transition is consistent with decreasing FSI contributions and gives us for the first time a direct access to the high momentum component of the deuteron momentum distribution. We find that within the MS model the calculations using the CD-Bonn potential are in best agreement with the data.

We acknowledge the outstanding efforts of the staff of the Accelerator and Physics Divisions at Jefferson Lab who made this experiment possible. This work was supported in part by the Department of Energy under contracts DE-FG02-99ER41065, DE-AC02-06CH11357, the Italian Istituto Nazionale di Fisica Nucleare, the French Centre National de la Recherche Scientifique and the National Science Foundation. Jefferson Science Associates (JSA) operates the Thomas Jefferson National Accelerator Facility for the U.S. Department of Energy under contract DE-AC05-84ER40150.

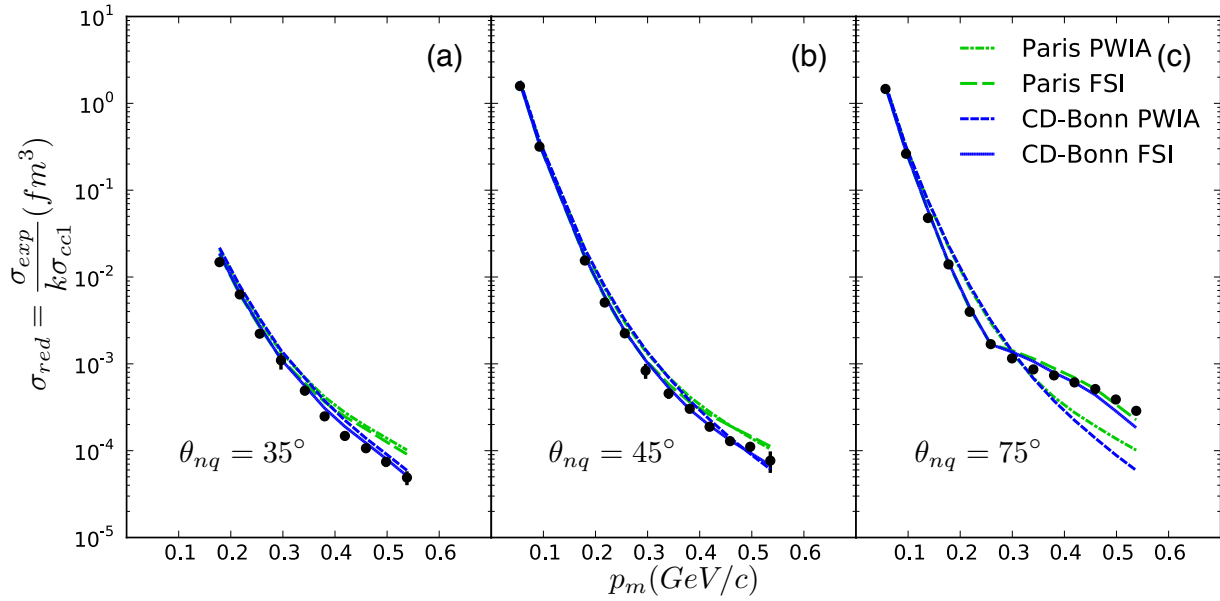


FIG. 2: (Color online) The reduced cross section $\sigma_{red}(p_m)$ as a function of missing momentum p_m is shown in panels a, b and c for $\theta_{nq} = 35^\circ, 45^\circ$ and 75° , respectively, and a bin width of $\pm 5^\circ$. CD-Bonn potential: dashed (blue) lines PWIA, solid (blue) lines FSI. Paris potential: dash-dot (green) lines PWIA, long-dashed (green) lines FSI. The PWIA results are for all angles identical. All calculations are from the MS model[15, 19, 27].

-
- [1] L. C. Alexa et al., Phys. Rev. Lett. **65**, 1374 (1999).
 - [2] M. Garçon and J. W. Van Orden, Adv. Nucl. Phys. **26**, 293 (2001).
 - [3] R. Gilman and F. Gross, J. Phys. G **28**, R37 (2002).
 - [4] P. E. Bosted, R. G. Arnold, S. Rock, and Z. M. Szalata, Phys. Rev. Lett. **49**, 1380 (1982).
 - [5] S. Rock et al., Phys. Rev. D **46**, 24 (1992).
 - [6] J. R. Arrington, Ph.D. Thesis, California Institute of Technology, Pasadena (CA, USA) (1998), nucl-ex/0608013.
 - [7] J. Arrington et al., Phys. Rev. Lett. **82**, 2056 (1999).
 - [8] O. Benhar, A. Fabrocini, S. Fantoni, V. Pandharipande, and I. Sick, Phys. Rev. Lett. **69**, 881 (1992).
 - [9] L.L. Frankfurt et al., Phys. Rev. C **48**, 2451 (1993).
 - [10] A. Bussiere et al., Nucl. Phys. A **365**, 349 (1981).
 - [11] K.I. Blomqvist et al., Phys. Lett. B **429**, 33 (1998).
 - [12] W. Boeglin et al., Phys. Rev. C **78**, 054001 (2008).
 - [13] P.E Ulmer et al., Phys. Rev. Lett. **89**, 062301 (2002).
 - [14] M. Rvachev, F. Benmokhtar, E. Penel-Nottaris, et al., Phys. Rev. Lett. **94**, 192302 (2005).
 - [15] M. M. Sargsian, Int. J. Mod. Phys. E **10**, 405 (2001).
 - [16] M. M. Sargsian et al., J. Phys. G **29**, R1 (2003).
 - [17] A. Bianconi, S. Jeschonnek, N. N. Nikolaev, and B. G. Zakharov, Phys. Lett. B **343**, 13 (1995).
 - [18] L.L. Frankfurt, W.G. Greenberg, J.A. Miller, M.M. Sargsian, and M.I. Strikman, Z. Phys. A **352**, 97 (1995).
 - [19] L.L. Frankfurt, M.M. Sargsian, and M.I. Strikman, Phys. Rev. C **56**, 1124 (1997).
 - [20] S. Jeschonnek, Phys. Rev. C **63**, 034609 (2001).
 - [21] C. Ciofi degli Atti and L. P. Kaptari, Phys. Rev. Lett. **100**, 122301 (2008).
 - [22] S. Jeschonnek and J. W. Van Orden, Phys. Rev. C **78**, 014007 (2008).
 - [23] S. Jeschonnek and J. W. Van Orden, Phys. Rev. C **80**, 054001 (2009).
 - [24] L. P. Kaptari and C. Ciofi degli Atti, Phys. Rev. C **71**, 024005 (2005).
 - [25] J.M. Laget, Phys. Lett. B **609**, 49 (2005).
 - [26] S. Jeschonnek and J. W. Van Orden, Phys. Rev. C **81**, 014008 (2010).
 - [27] M. Sargsian, Phys. Rev. C **82**, 014612 (2010).
 - [28] K. S. Egiyan et al., Phys. Rev. Lett. **98**, 26502 (2007).
 - [29] John Alcorn et al., NIMA **522**, 294 (2004).
 - [30] J. Arrington, Phys. Rev. C **69**, 022201(R) (2004).
 - [31] V. L. Rvachev and T. I. Sheiko, Appl. Mech. Rev. **48**, 151 (1995).
 - [32] <http://hallaweb.jlab.org/software/mceep/mceep.html> (2006).
 - [33] https://hallcweb.jlab.org/wiki/index.php/Monte_Carlo (2009).
 - [34] R. Ent, B. W. Filippone, N. C. R. Makins, R. G. Milner, T. G. O'Neill, and D. A. Wasson, Phys. Rev. C **64**, 054610 (2001).
 - [35] T. de Forest, Nucl. Phys. A **392**, 232 (1983).
 - [36] A. Saha, E. Voutier, et al., Jefferson Lab Proposal **PR02-105** (2002).